

# **Signal Processing Requirements are Dominated by RFI Concerns at the ATA**

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Acknowledgements: G. C. Bower, L. R. D'Addario, M. M. Davis, D. R. DeBoer, J. W. Dreher, G. Girmay-Kaletka, W. L. Urry, and M. C. H. Wright

ATA  $10^4 \text{ m}^2$



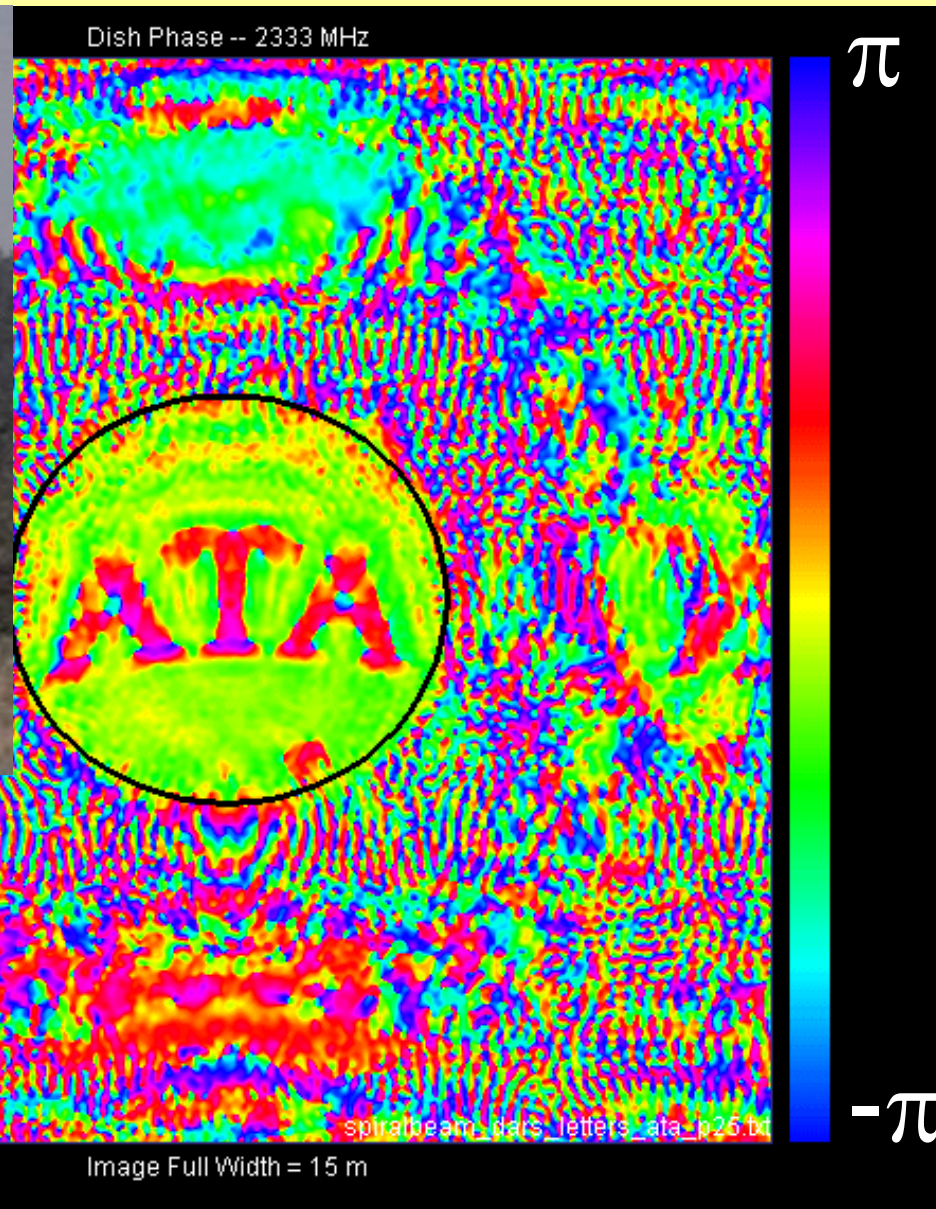
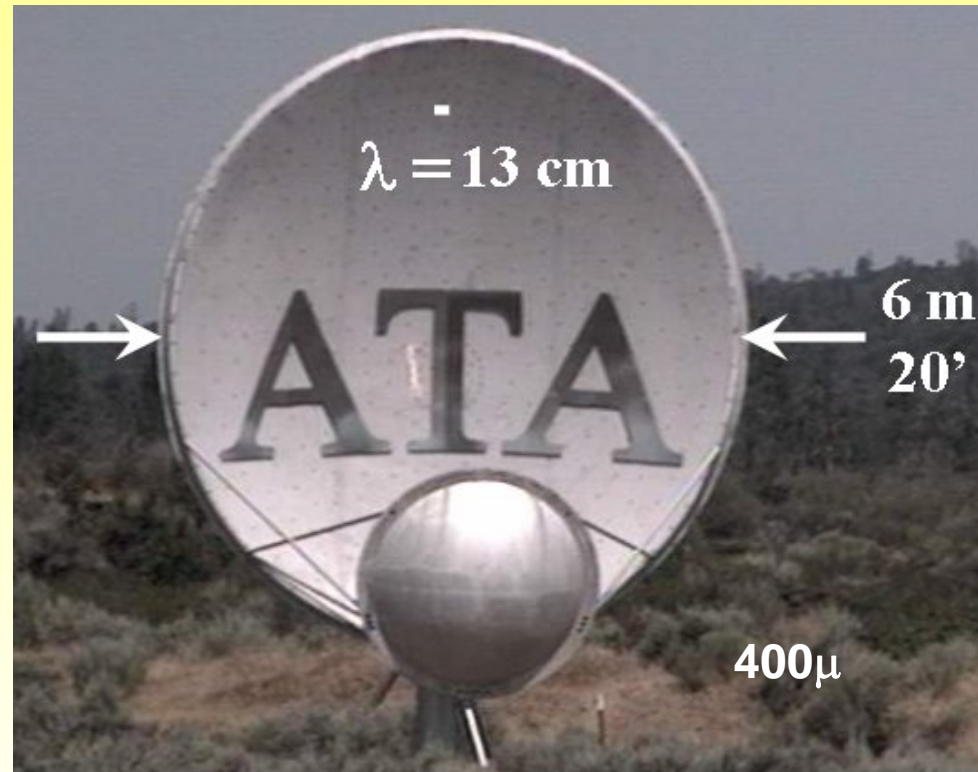
350 x 6m dishes  
RF = 0.5 – 11.2  
GHz

IF = 4 x 100 MHz

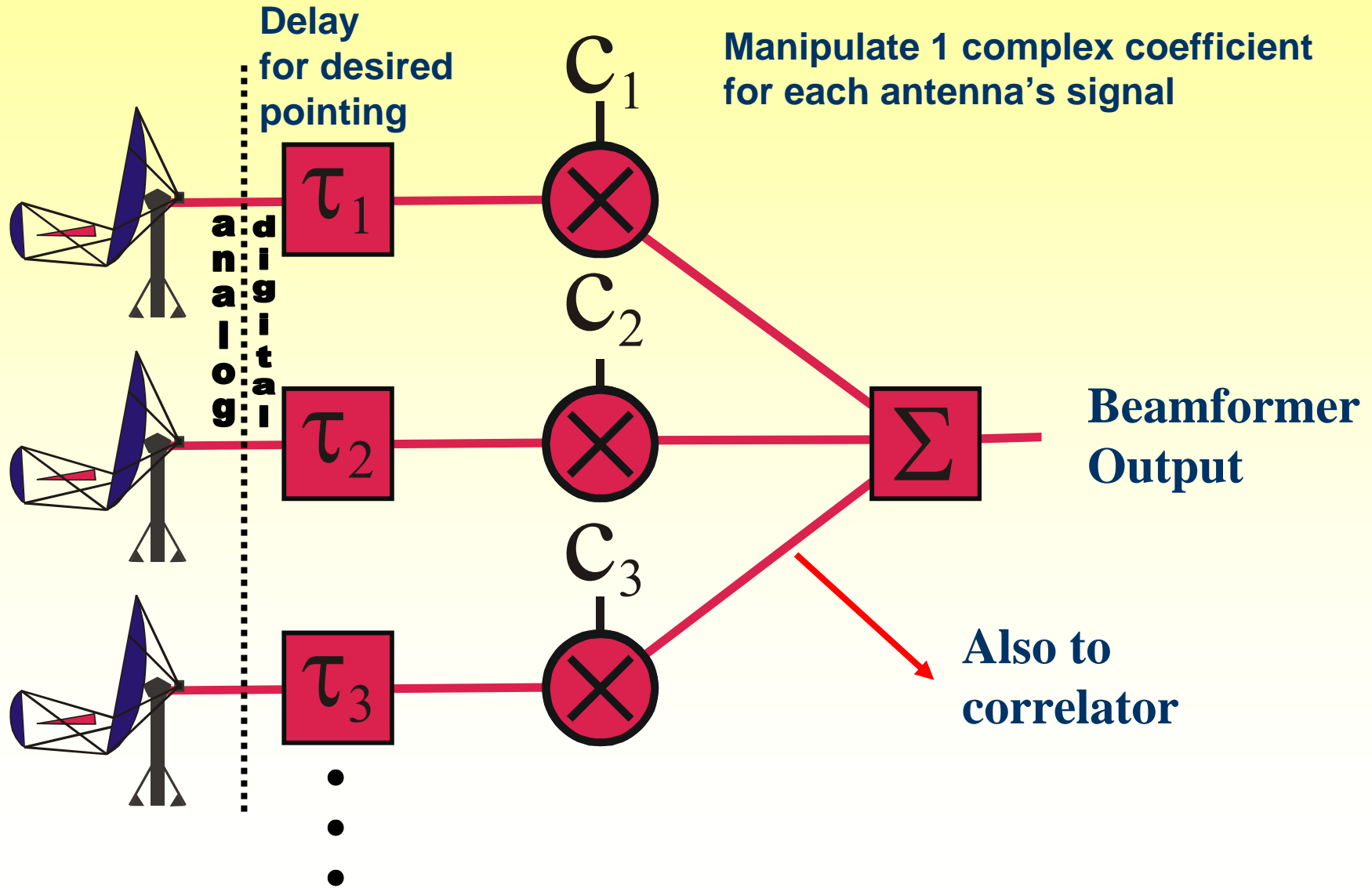
Funded by Paul  
Allen and Nathan  
Myhrvold

Developed jointly  
by SETI Institute  
and U. C. Berkeley  
RAL

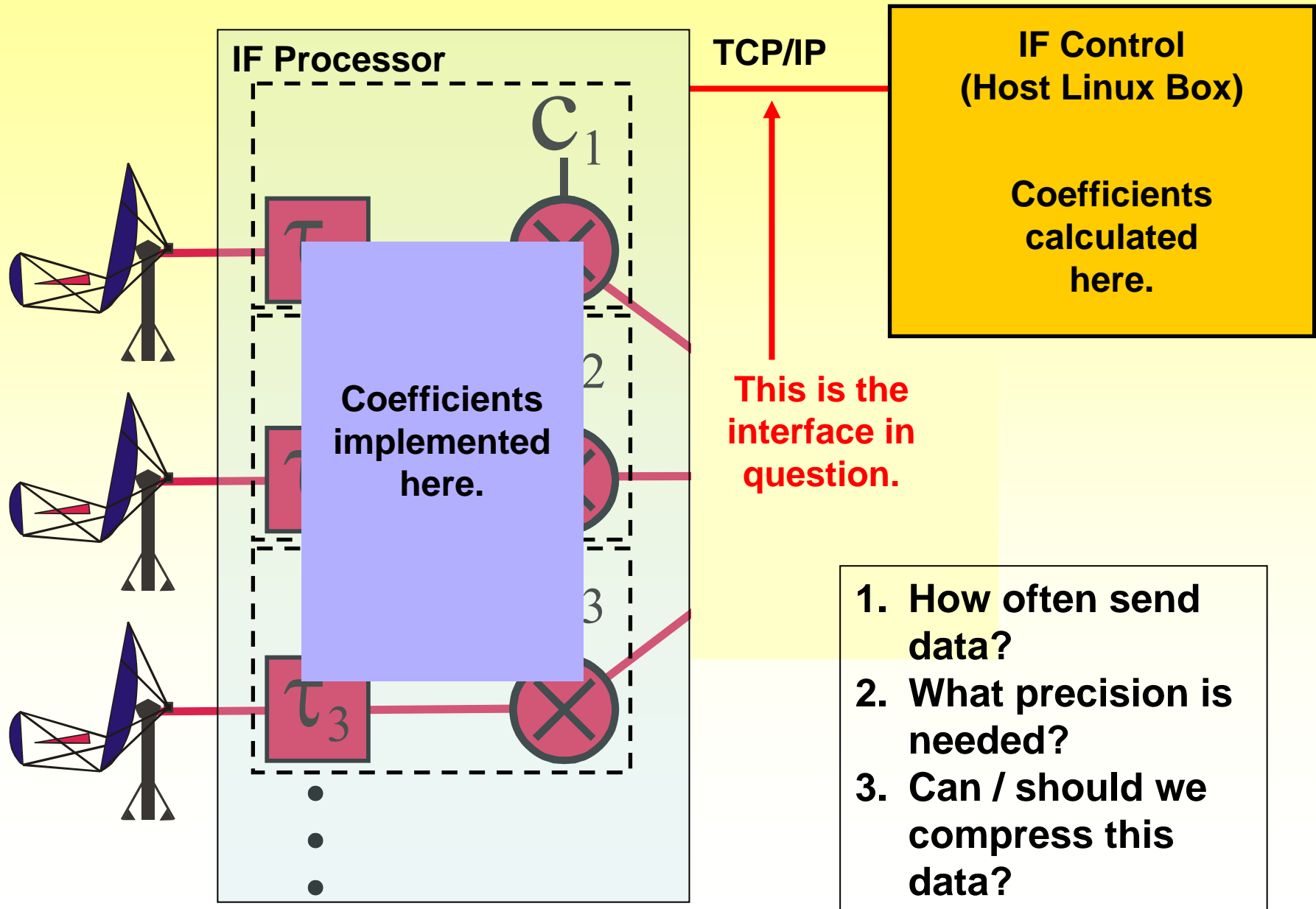
# ATA Dish at 13 cm



# DSP: IF Processor



# IF Processor Control Interface



# Track a moving source.

$$B(t) = \sum_i c_i s_i(t - \tau_i), \text{ where}$$

$s_i$  = signal at antenna  $i$

$c_i$  = beamformer coefficient =  $e^{-i\vec{k} \cdot \vec{r}_i}$

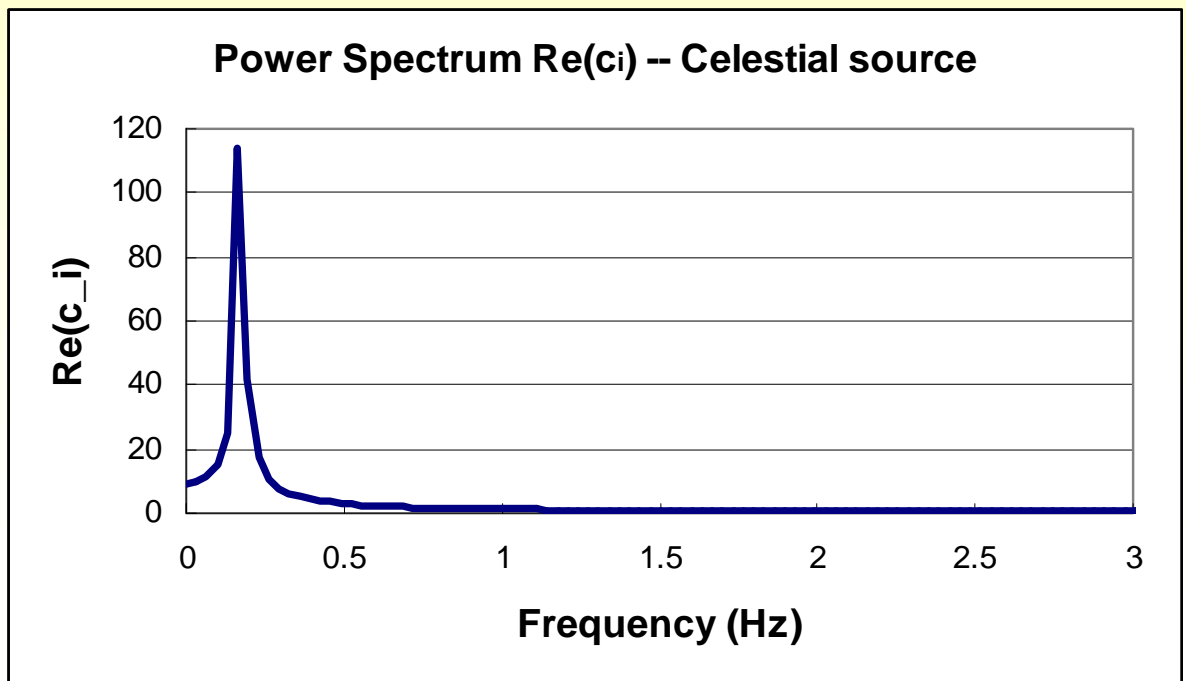
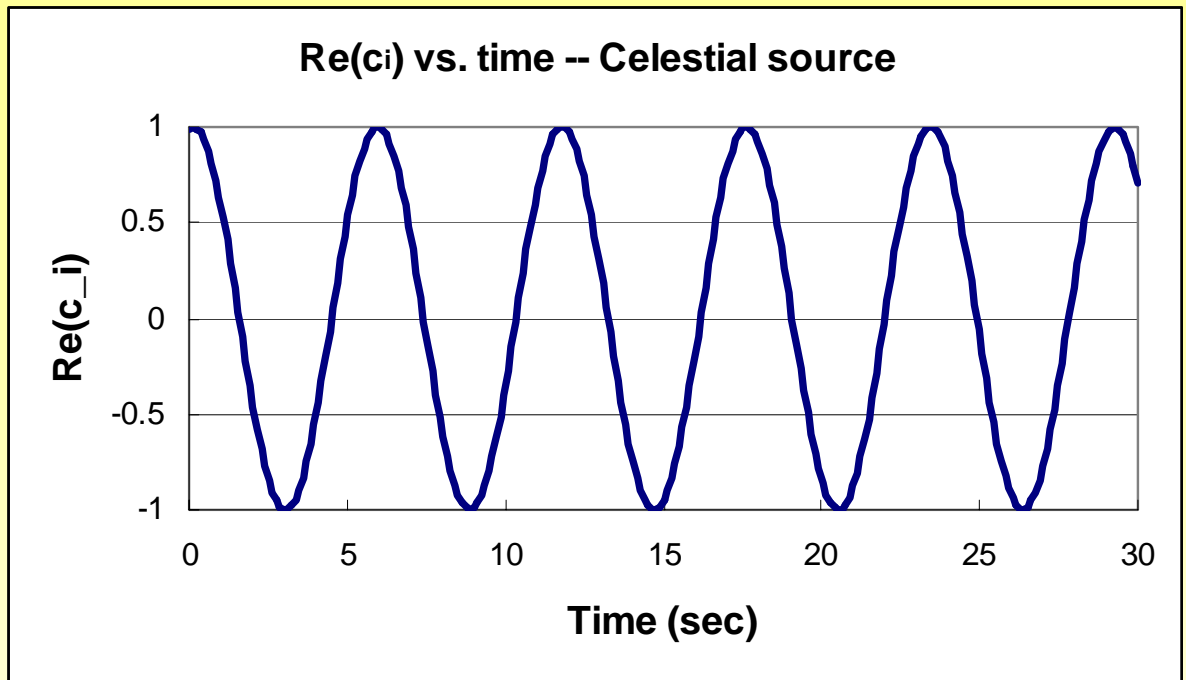
Suggested representation :

let  $\vec{k}(t) \approx \vec{k}_0 + \vec{k}_1 t + \dots$

→  $\text{Re}(c_i)$  is sine wave.

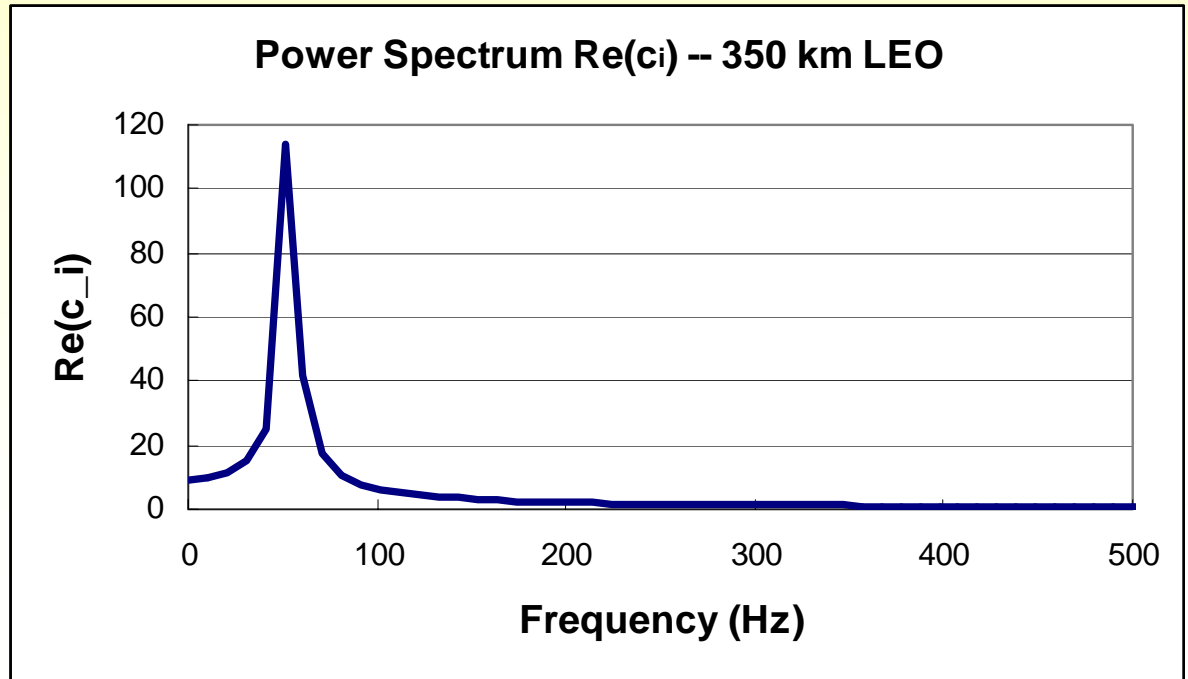
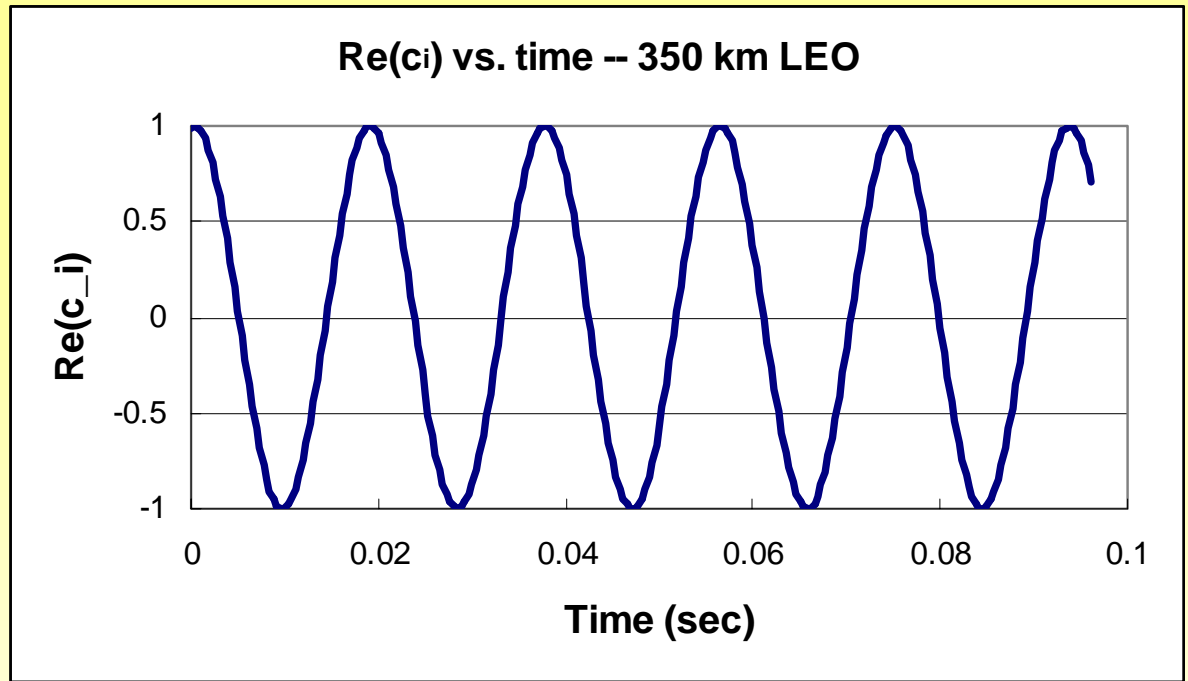
Tracking a  
celestial  
source at  
10 GHz.

0.16 Hz  
typical



Tracking  
a 350  
km LEO  
at  
10 GHz.

50 Hz  
typical





# Our first analysis.

- Nulling a LEO is about as hard as tracking a LEO
- Expand coefficients as Taylor's series

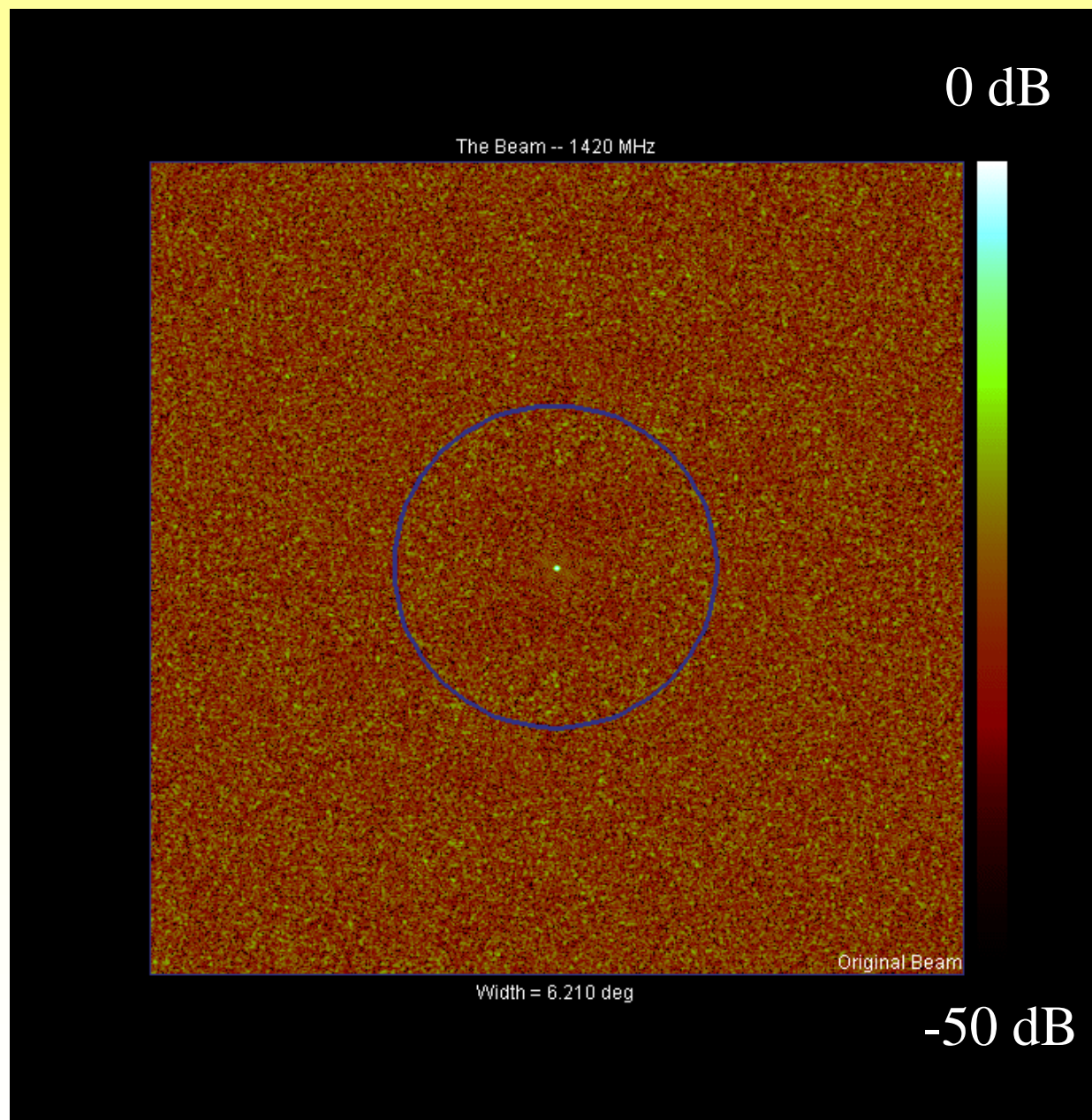
$$c_i = \alpha_i(t) e^{-i\vec{k}\cdot\vec{r}_i}$$

$$\alpha(t) = \alpha_0 + \alpha_1 t, \quad \vec{k} \approx \vec{k}_0 + \vec{k}_1 t + \vec{k}_2 t^2$$

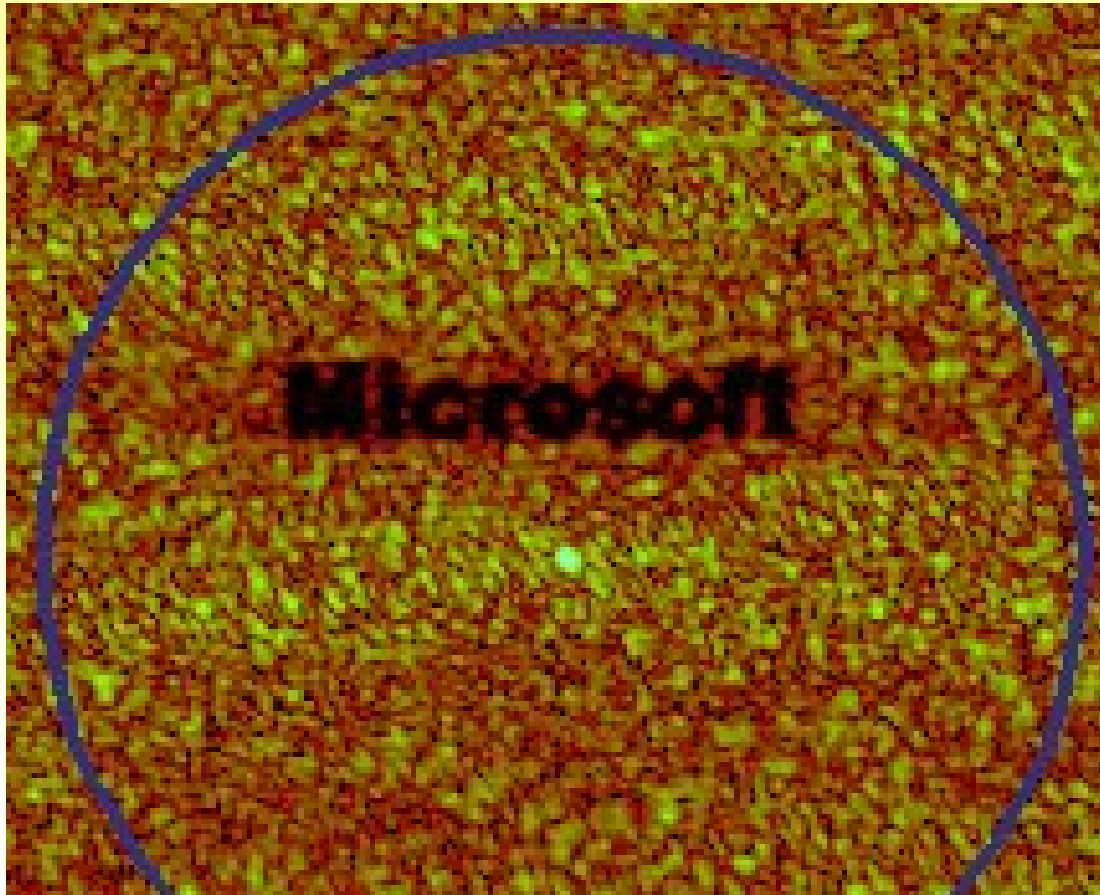
- This representation is good for about 0.2 seconds, even for LEO's
- Check this with simulations

# Synthetic Beam Pattern

We've been working on methods to form (wide bandwidth) deterministic nulling in Single Tap Beamformer.

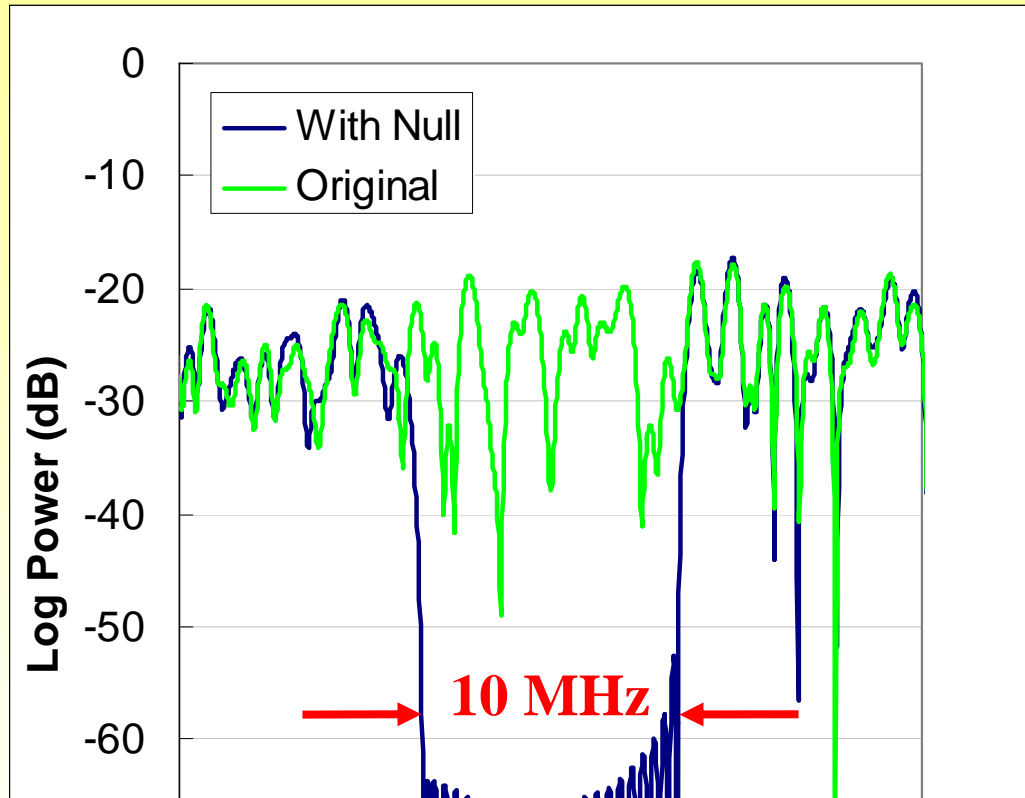


**Place beamformer nulls on the sky where  
satellites appear.**



**With 350 Antennas, we have lots of  
flexibility.**

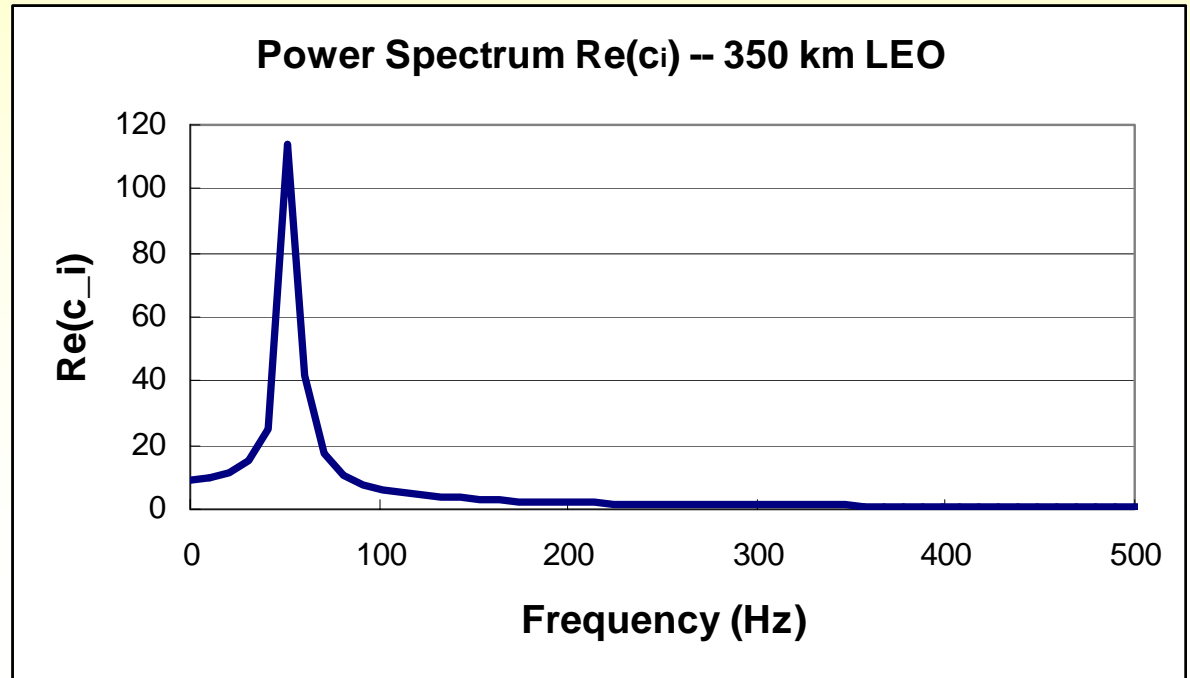
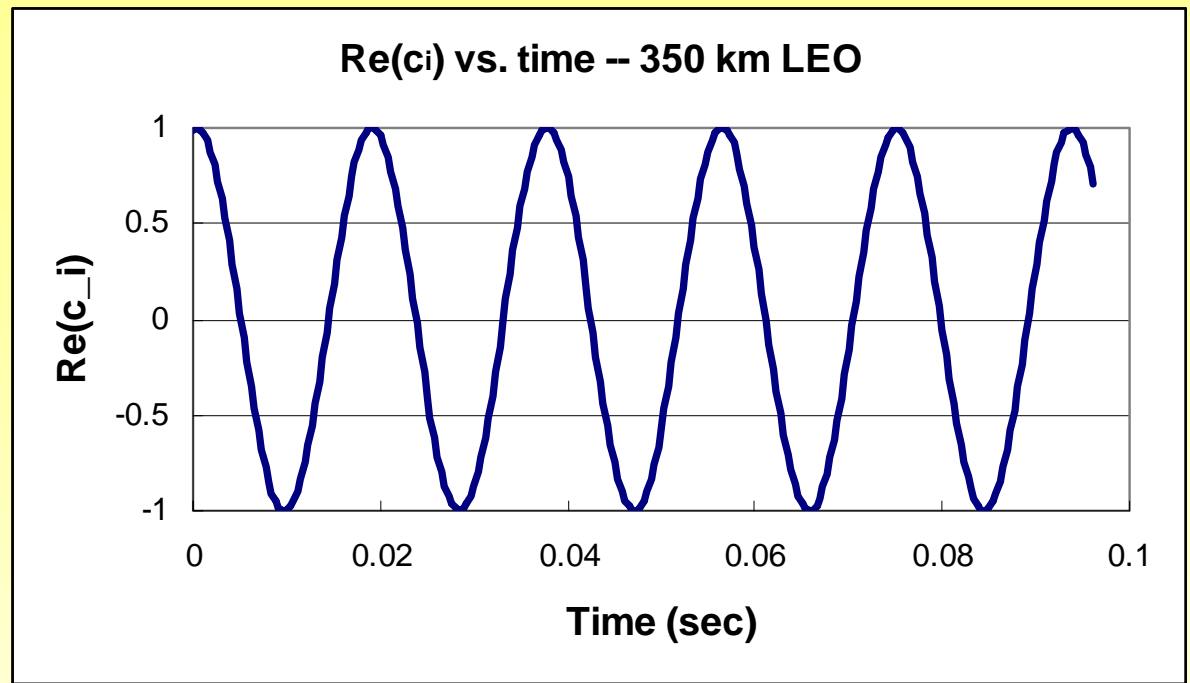
# We've developed methods for wideband nulls in single-tap beamformer, too.



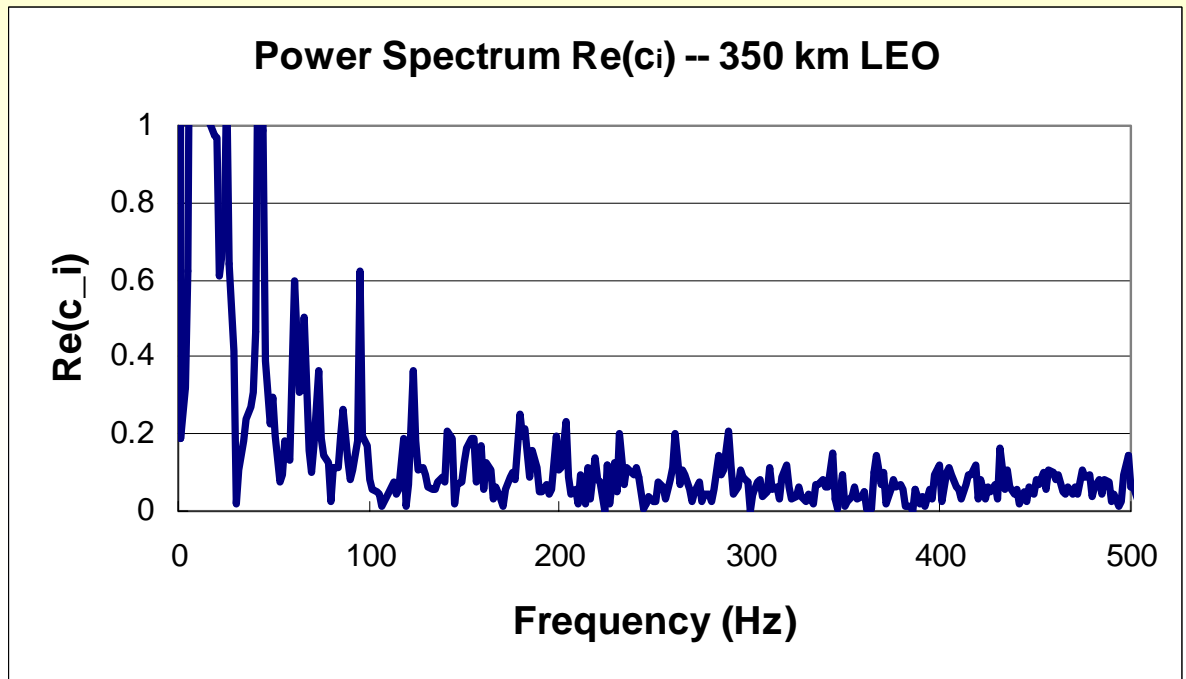
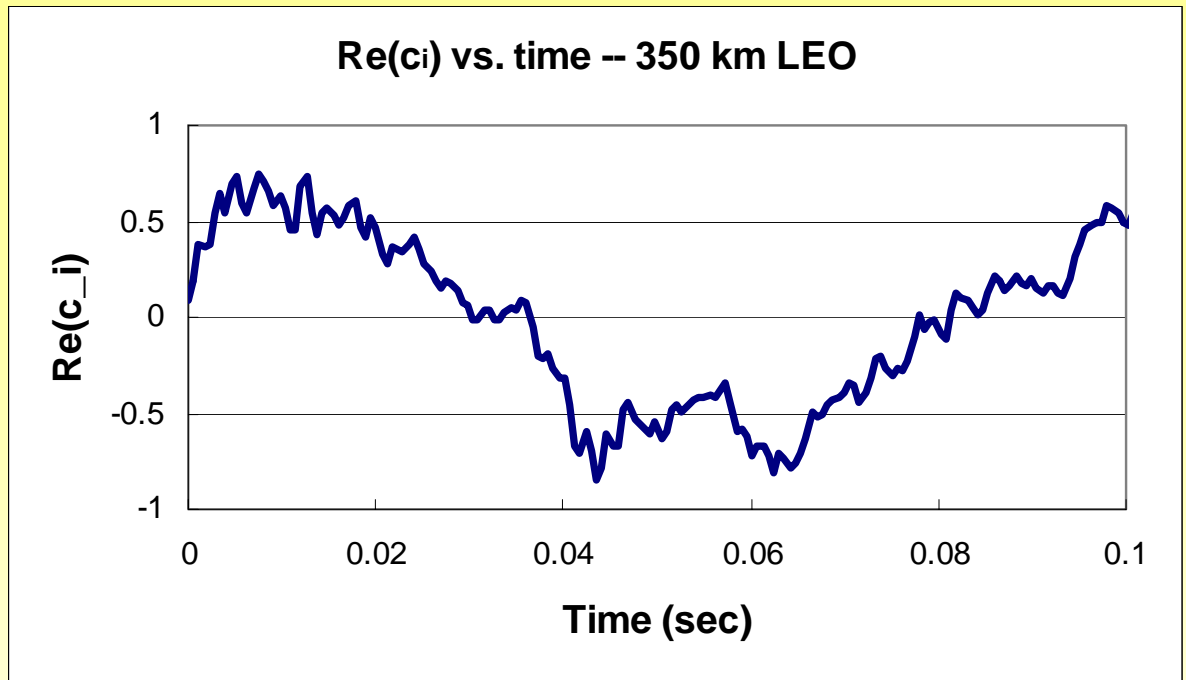
**Coefficients for deterministic nulls have same temporal structure as those for adaptive nulling or for post-correlation processing.**

Tracking  
a 350  
km LEO  
at  
10 GHz.

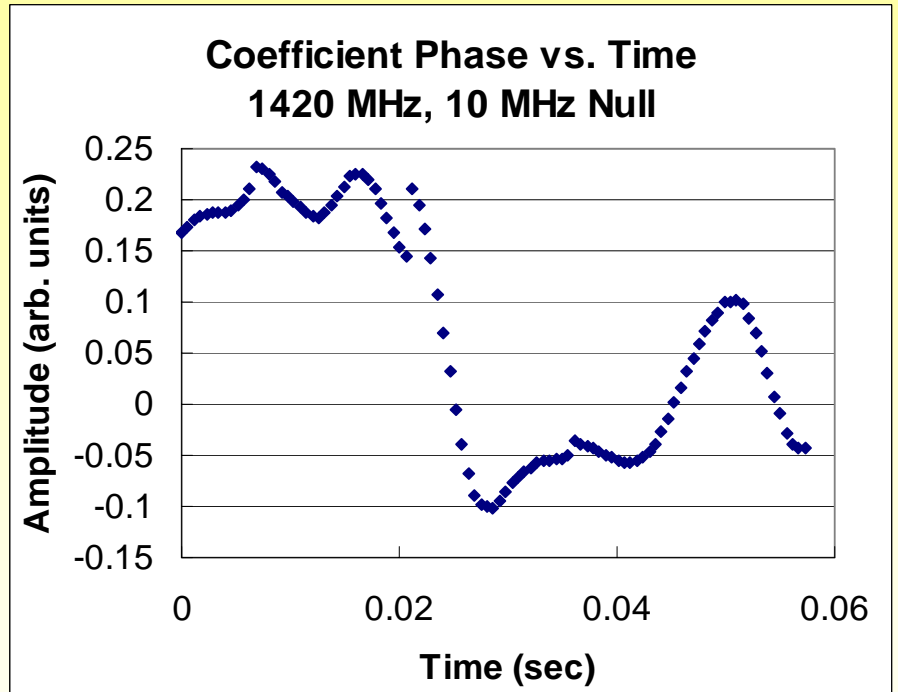
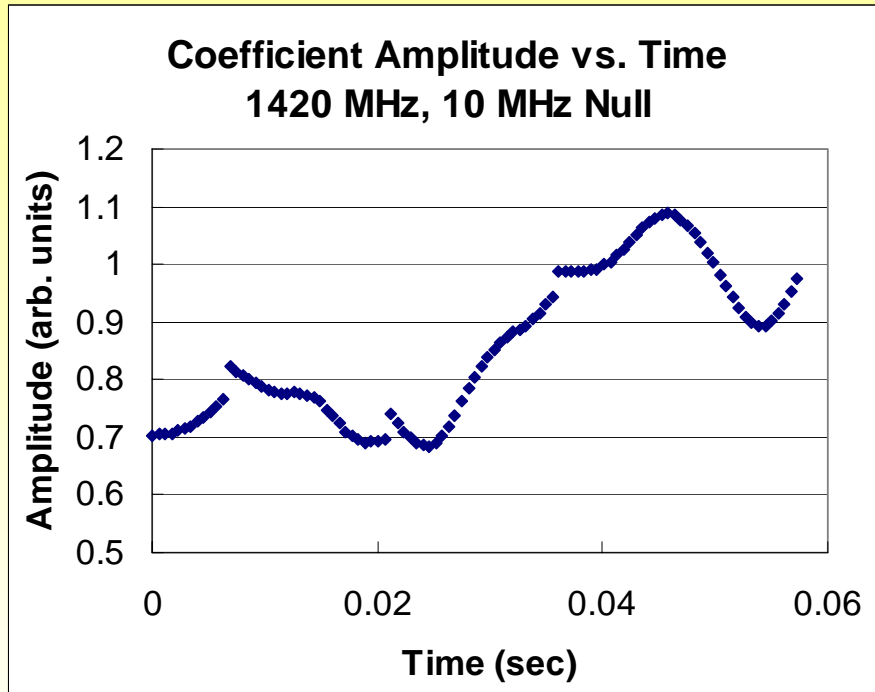
50 Hz  
typical



Tracking  
a 350  
km LEO  
at  
10 GHz.  
  
nothing  
typical!



# $c(t)$ shows near-discontinuities



$$\vec{k} \approx \vec{k}_0 + \vec{k}_1 t + \vec{k}_2 t^2 + \dots$$

is a bad approximation.

# Correct analysis.

- $c_i$  contains a SUM over frequencies

$$B_{S-I} = \sum_i e^{-i\vec{k}_S \cdot \vec{x}_i} \left[ 1 - \frac{e^{i\vec{k}_I \cdot \vec{x}_i}}{N} \sum_j e^{-i\vec{k}_I \cdot \vec{x}_j} \right] S_i$$

- Taylor's series is advantageous to no higher than 2 terms, good for 0.001 sec.

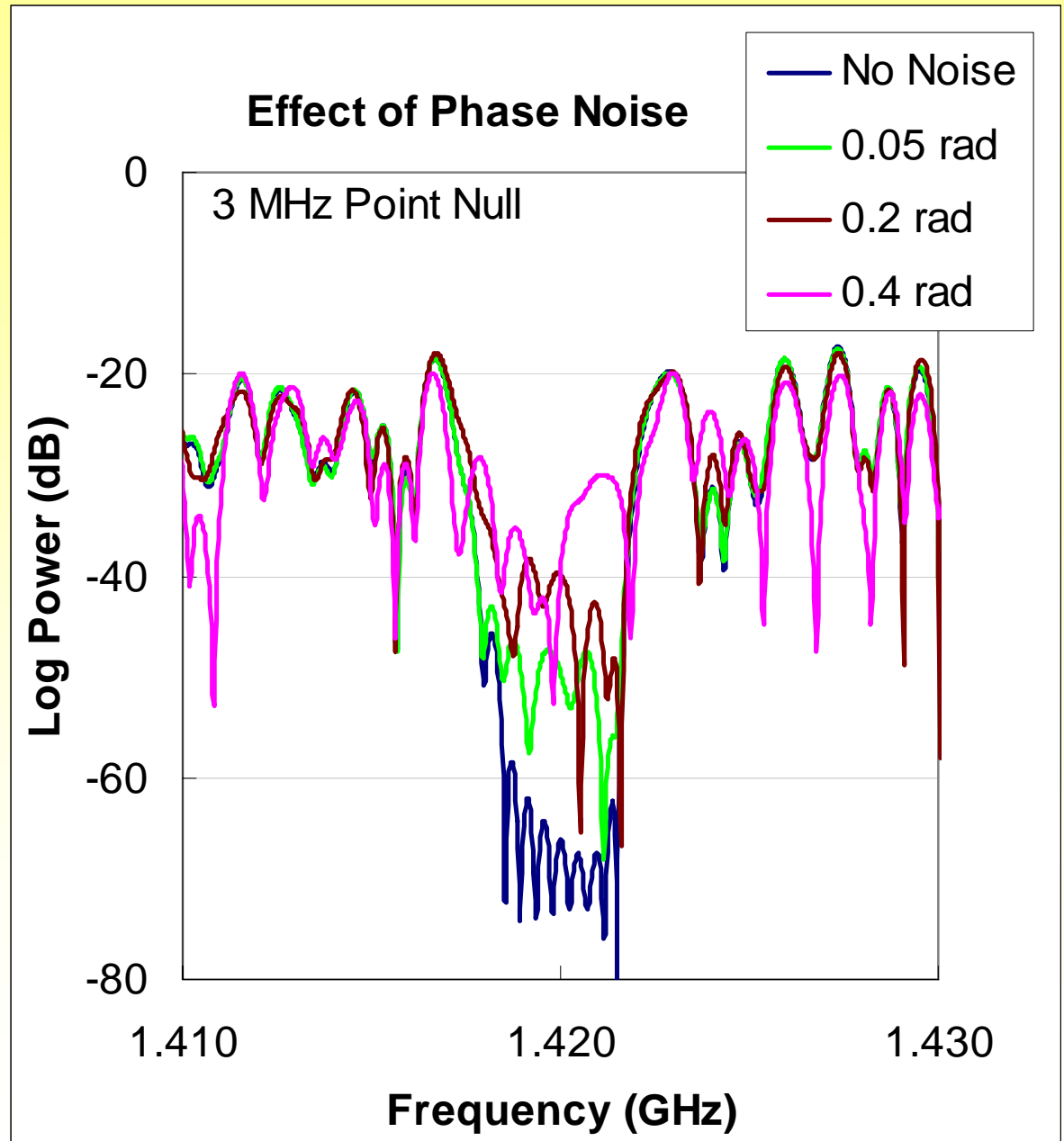
$$c_i = (\text{Re}(c_i), \text{Im}(c_i)), \quad c_i = c_{i,0} + c_{i,1} t + \dots$$

**200x harder than we first thought!**



Simulations  
also tell us the  
numerical  
precision and  
accuracy  
required.

1° phase  
accuracy  
needed



# Extrapolate to SKA

- Max update frequency: 
$$\nu_{\max} = \frac{2dfv}{ch}$$
where

$d$  = array size,  $f$  = max observation frequency

$v$  = LEO velocity = 8 km/s

$h$  = LEO height,  $c$  = light speed

- $\nu_{\max} = 900$  Hz at ATA = correlator dump rate
- $\nu_{\max} \sim 1$  MHz at SKA (BF and Corr)
- $0.01^\circ$  precision

Come and see our poster:

“Using Multiple Beams to Distinguish RFI  
from ETI Signals”

This and other work:

[www.gerryharp.com](http://www.gerryharp.com)

ATA memo series:

[intranet.seti.org/ata](http://intranet.seti.org/ata)

Ask me for site/password